

Comprehensive investigation on extremely low lattice thermal conductivity and thermoelectric properties of BaIn_2Te_4

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Abstract

Recently, extremely low lattice thermal conductivity value has been reported for alkali based telluride material, BaIn_2Te_4 . The value is comparable with low-thermal conductivity metal chalcogenides and the glass limit is highly intriguing. Therefore, to shed light on this issue, we performed first-principles phonon thermal transport calculations. We predicted highly anisotropic lattice thermal conductivity along different directions by the solution of linearized phonon Boltzmann transport equation. More importantly, we determined several different factors as the main sources of the predicted ultralow lattice thermal conductivity of this crystal, such as the strong interactions between low-frequency optical phonons and acoustic phonons, small phonon group velocities, and lattice anharmonicity indicated by large negative mode Grüneisen parameters. Along with thermal transport calculations, we also investigated the electronic transport properties by accurately calculating the scattering mechanisms, namely, acoustic deformation potential, ionized impurity, and polar optical scatterings. The inclusion of spin-orbit coupling (SOC) for electronic structure is found to be strongly affect the p -type Seebeck coefficients. Finally, we calculated the thermoelectric properties accurately and the optimal ZT value of p -type doping, which originated from high Seebeck coefficients, was predicted to exceed unity after 700 K and have a direction averaged value of 1.63 (1.76 at y -direction) at 1000 K around $2 \times 10^{20} \text{ cm}^{-3}$ hole concentration. For the n -type doping, the ZT around $3.2 \times 10^{19} \text{ cm}^{-3}$ concentration was predicted to be as direction averaged value of 1.40 (1.76 at z -direction) at 1000 K, mostly originating from its high electron mobility. With the experimental evidence of high thermal stability, we showed that the BaIn_2Te_4 compound has the potential for being a promising mid-to-high temperature thermoelectric material for both p -type and n -type systems with appropriate doping.

Keywords: thermoelectric materials, thermal conductivity, density functional theory, Boltzmann transport equation

I. INTRODUCTION

For many years, tellurium-based thermoelectric materials have been extensively studied due to their high Seebeck coefficients, low thermal conductivity, and resulting high figure of

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merit. Among them, Bi_2Te_3 [1] and PbTe [2, 3] are the most well known ones for their good thermoelectric performance. Based on this potential, many ternary telluride materials such as chalcopyrites[4–7], thallium-based materials[8–11], and other complex materials[12–14] have been also studied for their thermoelectric properties. Also, complex thermoelectric materials[15] known to have large number of atoms and atomic species in their unit cells with low symmetry and usually exhibit low thermal conductivity have been considered. Skutterudites[16, 17], clathrates[18], and Zintl phases[19, 20] are well known families of these type of materials that satisfy the optimum balance for thermoelectric materials — the phonon-glass electron-crystal concept[21], where the electrons of a thermoelectric material are expected to behave like metals and the phonons (vibrational modes) behave like glasses.

To satisfy the optimum balance in the bulk materials scale, the alkali-based AB_2Te_4 (A=Mg, Ca, Sr, Ba and B=Al, Ga, In) family, as a specific class of telluride compounds, has been synthesized for decades[22–28] and has become an emerging class of materials for their potential in thermoelectric applications[25–27, 29]. For some of these tellurides possessing diverse crystal structures such as cubic[29], tetragonal[22–24], orthorhombic[25, 27, 28], and triclinic[23] and promising results have been reported.

Recently, Ishtiyak *et. al.*[27] have experimentally reported that the orthorhombic BaIn_2Te_4 exhibits extremely low thermal conductivity as 0.30 W/mK at 965 K. Intriguingly, the value, comparable with low-thermal conductivity metal chalcogenides and the glass limit, is one of the lowest value reported for this class of materials[25, 26]. Thermoelectric properties of the undoped polycrystalline samples of BaIn_2Te_4 material were also investigated experimentally in the same study. Despite the predicted extremely low lattice thermal conductivity, the thermoelectric performance of this material was measured as quite low, with $ZT = 0.06$ at 965 K. However, the measured low value was attributed not to the potential of the material but to the very low intrinsic doping (carrier concentration) of the prepared samples. The strategies such as spark plasma sintering and chemical doping were proposed to improve the corresponding thermoelectric efficiency. Therefore, it is worth predicting the potential of this material as thermoelectric prior to further experimental investigations.

On the other hand, the BaIn_2Te_4 , having 14 atoms in its primitive cell, is a semiconducting alkali telluride with orthorhombic $Cccm$ structure and has one-dimensional (1D) chains of distorted tetrahedrons. These tetrahedrons contain indium atoms surrounded by

tellurium atoms and reside together with weakly-bonded barium atoms in a cage-like framework. The central indium atoms align in a distorted zig-zag structure and result in a notable effect on both electron and phonon transport [30–32]. In that sense, transport and thermoelectric properties of these materials are anisotropic and highly accurate approaches require to investigate direction-dependent transport properties.

Therefore, in this study, using phonon Boltzmann Transport and electron-phonon coupling approaches based on first-principles calculations, we investigated the thermal and electronic transport properties of BaIn_2Te_4 . We found that calculated thermal conductivity is in perfect agreement with the experiment. Together with large Seebeck coefficients of hole-doping (p -type), we predicted considerably high performance with an average ZT value, 1.63 at 1000 K. The mobility of electron-doping (n -type) was found to be much larger than that of hole-doping and the average ZT for that case was calculated as 1.40 at 1000 K.

II. COMPUTATIONAL DETAILS

All the first principles calculations were performed using the Vienna Ab-initio Simulation Package (VASP) [33] which is based on density functional theory [34, 35] in the framework of plane-wave pseudopotential method. The interaction between ions and electrons were described with projector augmented wave (PAW) pseudopotentials [36], considering the Ba $5s$ $5p$ $6s$, In $4d$, $5s$, $5p$, and Te $5s$, $5p$ states as valence states. Perdew-Burke-Ernzerhof (PBE) [37] parameterization were adopted for the exchange and correlation functional which is based on the generalized gradient approximation (GGA). We have also included spin-orbit coupling interaction in the structural and electronic structure calculations and its effects on electronic and thermoelectric properties were compared with the pure GGA-PBE results. In order to obtain more reliable estimation of the band gap, Heyd–Scuseria–Ernzerhof (HSE06)[38] type hybrid functional was used.

An energy cut-off value of 400 eV was found to be converged for plane waves, and a convergence criterion of 10^{-7} eV was taken for self-consistent field calculations. In the geometric optimization calculations, the residual forces acting on each atom was relaxed with a criterion of 10^{-4} eV/Å. For the total energy and geometric optimization calculations, a converged $6 \times 6 \times 3$ k -grid was used and a denser $12 \times 12 \times 6$ grid was chosen for the subsequent calculations of the electronic density of states and thermoelectric coefficients.

Second-order interatomic force constants (IFCs) and subsequently the phonon dispersion curves and the phonon density of states were obtained within supercell finite difference method as implemented in Phonopy code[39]. We used $2 \times 2 \times 2$ supercells and a $3 \times 3 \times 2$ k-point grid for second-order IFCs. Third-order force constants were calculated with thirddorder.py script[40], which also uses the finite difference method. In these calculations, $3 \times 3 \times 2$ supercell as cell size, single Γ centered k -point as reciprocal space grid, fourth nearest neighbors as a maximum atomic interaction distance, and 0.01 Å as displacement of atomic perturbations were considered.

Phonon transport properties were obtained with ShengBTE[40] code, which solves linearized phonon Boltzmann transport equations (BTE). Apart from phonon-phonon scatterings, the phonon-isotope scattering from the naturally occurring isotope concentrations were also included. In the ShengBTE calculations, for the q -grid convergence, calculations were performed for the scalebroad[40] parameters 1.0 and 0.1 on a $12 \times 12 \times 9$ grid. The final calculations were performed with the value scalebroad=0.1 on a $16 \times 16 \times 12$ q -grid, those result in ($\sim 2\%$) difference in convergence calculations.

Electron transport properties such as electrical conductivity, electronic thermal conductivity, and Seebeck coefficients have been calculated in the framework of AMSET[41] code which uses momentum relaxation time approximation (MRTA) in order to calculate scattering rates and mobilities within Born approximation. In the AMSET code, relaxation times are estimated by a number of different band and k -point dependent scattering processes instead of constant relaxation time approach as implemented in widely used BoltzTraP code[42, 43]. Among these processes, acoustic deformation potential (ADP) scattering is responsible for acoustic phonon-electron interactions. Ionized impurity scattering (IMP) represents the scattering of charge carriers by ionization of the lattice. Interactions between polar optical phonons and electrons are named as polar optical scattering (POP). One other scattering mechanism also implemented in AMSET code is the piezoelectric scattering (PIE) which considers the coupling between acoustic waves and charge carriers that induced by macroscopic electric fields created by the elastic strain. We omit piezoelectric scattering in our calculations because the BaIn_2Te_4 material belongs to the centrosymmetric $Cccm$ space group[27] and the piezoelectric moduli vanish. The resulting electronic relaxation times (τ) (the inverse of scattering rates) of the considered scattering processes can be written by

following the Matthiessen's rule:

$$\frac{1}{\tau} = \frac{1}{\tau_{\text{ADP}}} + \frac{1}{\tau_{\text{IMP}}} + \frac{1}{\tau_{\text{POP}}} + \frac{1}{\tau_{\text{PIE}}}. \quad (1)$$

The ADP, IMP, and PIE scatterings are described as elastic scattering where electrons do not gain or lose energy in these type of scattering processes. For the POP type processes, inelastic scattering occurs because of a phonon emission or absorption. The AMSET code uses the momentum relaxation time approximation for the elastic scatterings and self-energy relaxation time approximation for the inelastic scatterings.

The scattering rates for the elastic scatterings from an initial $n\mathbf{k}$ state to $m\mathbf{k} + \mathbf{q}$ final state can be written using the Fermi golden rule[41]:

$$\tau_{n\mathbf{k} \rightarrow m\mathbf{k} + \mathbf{q}}^{-1} = \frac{2\pi}{\hbar} |g_{nm}(\mathbf{k}, \mathbf{q})|^2 \delta(\varepsilon_{n\mathbf{k}} - \varepsilon_{m\mathbf{k} + \mathbf{q}}) \quad (2)$$

and for the inelastic scattering rate a similar type of equation is given as:

$$\begin{aligned} \tau_{n\mathbf{k} \rightarrow m\mathbf{k} + \mathbf{q}}^{-1} &= \frac{2\pi}{\hbar} |g_{nm}(\mathbf{k}, \mathbf{q})|^2 \\ &\times [(n_{\mathbf{q}} + 1 - f_{m\mathbf{k} + \mathbf{q}}^0) \delta(\Delta\varepsilon_{\mathbf{k}, \mathbf{q}}^{nm} - \hbar\omega_{\mathbf{q}}) \\ &+ (n_{\mathbf{q}} + f_{m\mathbf{k} + \mathbf{q}}^0) \delta(\Delta\varepsilon_{\mathbf{k}, \mathbf{q}}^{nm} + \hbar\omega_{\mathbf{q}})]. \end{aligned} \quad (3)$$

where \hbar is the reduced Planck constant, δ is the Dirac delta function, $\varepsilon_{n\mathbf{k}}$ is the energy of $|n\mathbf{k}\rangle$ state, n is the Bose-Einstein distribution, f is the Fermi-Dirac distribution, and the terms $-\hbar\omega_{\mathbf{q}}$ and $\hbar\omega_{\mathbf{q}}$ correspond to the phonon emission and absorption, respectively. The term $g_{nm}(\mathbf{k}, \mathbf{q})$ is the coupling matrix element of the considered scattering mechanism and the detailed form of the all scattering matrix elements are given in Ref. [41].

To obtain the scattering rates, all the required material parameters such as dense uniform band structures, wave function coefficients, elastic constants, deformation potentials, static and high-frequency dielectric constants and polar-phonon frequency were calculated from DFT and density functional perturbation theory (DFPT)[44]. Details of the calculated parameters are given in Supplemental Material Table S1[45]. The subsequent transport properties such as the Seebeck coefficient, electrical conductivity, and electronic thermal conductivity were calculated from the Onsager transport coefficients[42, 43]. During the AMSET calculations, a converged interpolation factor of 20 was used for GGA-PBE scheme which corresponds to a $49 \times 49 \times 25$ grid. For GGA-PBE-SOC, we have used a converged interpolation factor of 10 with a $53 \times 53 \times 27$ grid.

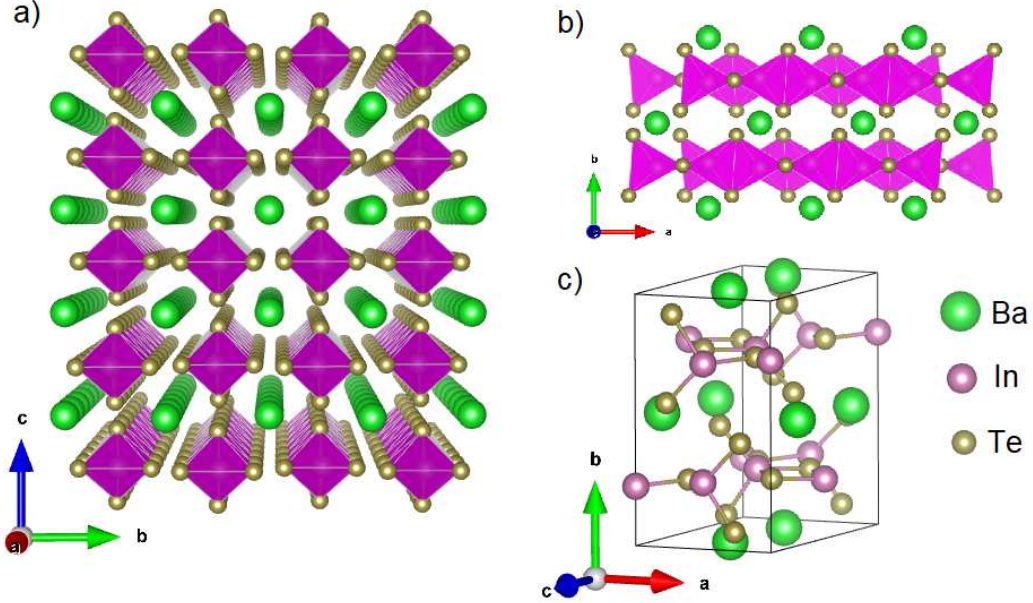


FIG. 1: Schematic view of orthorhombic BaIn_2Te_4 compound. (a) view in yz -plane, (b) view in xy -plane, and (c) the primitive cell. VESTA software[47] is used for visualization.

III. RESULTS

A. Structural properties

The BaIn_2Te_4 compound crystallizes in an orthorhombic lattice structure having the space group of $D_{2h}^{20} - Cccm$ (sp. gr. no 66). The schematic representation of the structure is given in Fig. 1. There exist 14 atoms in the primitive cell (Fig. 1c) as it is 2-fold according to the formula unit, where two of these atoms are barium, four are indium, and eight are tellurium atoms. The basis vectors[46] of BaIn_2Te_4 in reduced coordinates are given in Supplemental Material Table S2[45]. As shown in Figs. 1a and 1b, indium atoms that surrounded by four tellurium atoms compose tetrahedrals and form a 1D-like chain along a -axis (x -direction).

In Table I, equilibrium lattice parameters, internal parameters, bulk modulus, and pressure dependence of bulk modulus calculated with GGA-PBE and GGA-PBE-SOC are given along with available experimental results. As seen in Table I, the GGA-PBE and GGA-PBE-SOC results are very similar and the calculated equilibrium lattice parameters are larger than the experimental values with the typical overestimation of GGA. The calcu-

lated internal parameters are in good agreement with the experimentally reported X-ray diffraction measurements[27].

Bulk modulus and its pressure derivative are obtained by fitting the Birch-Murnaghan equation of state[48] (See Supplemental Material[45]). The results are also shown in Table I. To the best of our knowledge, there is no experimental or theoretical bulk modulus value in the literature for BaIn₂Te₄. The obtained bulk modulus $B = 18.45$ GPa is a relatively low value which are also reported in some other barium-containing materials[49, 50]. The pressure dependence of the bulk modulus $B'_0 = 4.46$ has been calculated and this value is typically found in the great majority of crystals.

B. Phonon properties and lattice thermal conductivity

For a deep understanding of lattice thermal conductivity, a detailed analysis of the vibrational and phonon transport properties is required. In this section, the extremely low thermal conductivity behavior of BaIn₂Te₄ will be explored by examining the phonon dispersion relations, phonon density of states, and phonon transport properties such as phonon

TABLE I: The GGA-PBE and GGA-PBE-SOC calculated lattice parameters, internal parameters, bulk modulus, and pressure derivative of bulk modulus compared with the available experimental results.

Parameter	GGA-PBE	GGA-PBE-SOC	Expt. (Ref.[27])
a (Å)	7.2598	7.2704	7.1417
b (Å)	12.314	12.312	12.034
c (Å)	12.445	12.443	12.107
z_2	0.82288	0.82263	0.82141
x_3	0.00196	0.00200	0.00156
y_3	0.26370	0.26372	0.26082
x_4	0.72792	0.72789	0.73918
y_4	0.42687	0.42707	0.42835
B_0 (GPa)	18.67	18.45	
B'_0	4.45	4.46	

group velocities, mode Grüneisen parameters, and scattering rates.

The lattice thermal conductivity at temperature T is given as:

$$\kappa_{\alpha\beta} = \frac{1}{k_B T^2 \Omega N} \sum_{\lambda} f_0(f_0 + 1) (\hbar \omega_{\lambda})^2 v_{\lambda}^{\alpha} F_{\lambda}^{\beta}, \quad (4)$$

where α and β are the Cartesian coordinates, k_B is the Boltzmann constant, Ω is the unit cell volume, N is the number of unit cells, f_0 is the equilibrium Bose-Einstein distribution function, ω_{λ} is the phonon frequency of the mode λ (representing the phonon branch index and wave number), and v_{λ} is the phonon group velocity. Here, F_{λ} is expressed as $F_{\lambda} = \tau_{\lambda}^0(v_{\lambda} + \Delta_{\lambda})$ where τ_{λ}^0 is the phonon relaxation time and Δ_{λ} is the correction term[40]. In the Relaxation Time Approximation (RTA) Δ_{λ} is set to be equal to zero. On the other hand, in the full consideration for the evaluation of Eqn. 4, F_{λ} is solved iteratively from linearized phonon Boltzmann Transport Equation as implemented in the ShengBTE code[40].

Phonon dispersion relations of BaIn_2Te_4 , calculated by solving the dynamical matrix that was obtained from 2^{nd} order force constants, are shown in Fig. 2 along the high symmetry directions of Γ -X-S-Y- Γ -Z of the Brillouin zone with including the LO/TO splitting. Since there exist 14 atoms in the primitive cell of the BaIn_2Te_4 material, there are total of 42 phonon modes for each \mathbf{q} -point where three of them are acoustic modes and the remaining 39 modes are optical modes. As shown in Fig. 2, all the phonon spectrum of BaIn_2Te_4 has positive frequencies in all directions, indicating a dynamically stable phase.

It is useful to note that acoustic branches have mostly low frequency values smaller than <1 THz. The flat acoustic branches at the most of the directions result low phonon group velocities and indicate low lattice thermal conductivity. Besides, low optical modes and LA acoustic modes strongly hybridize around 1 THz frequency region. This hybridization would provide more channels for phonon scattering and strongly suggests low lattice thermal conductivity. Although the dispersion of the majority of optical modes are flat, significant branches are noticeably dispersive in many frequency domains. The fact that the aforementioned high-branch optical modes have high group velocities, significant contributions to the lattice thermal conductivity are expected from these optical modes.

To determine the contributions of particular atoms to the phonon spectrum, we calculated the atom-projected phonon density of states and presented in Fig. 3. As can be seen from the figure, tellurium atoms contribute in all frequency domains. The contribution of barium

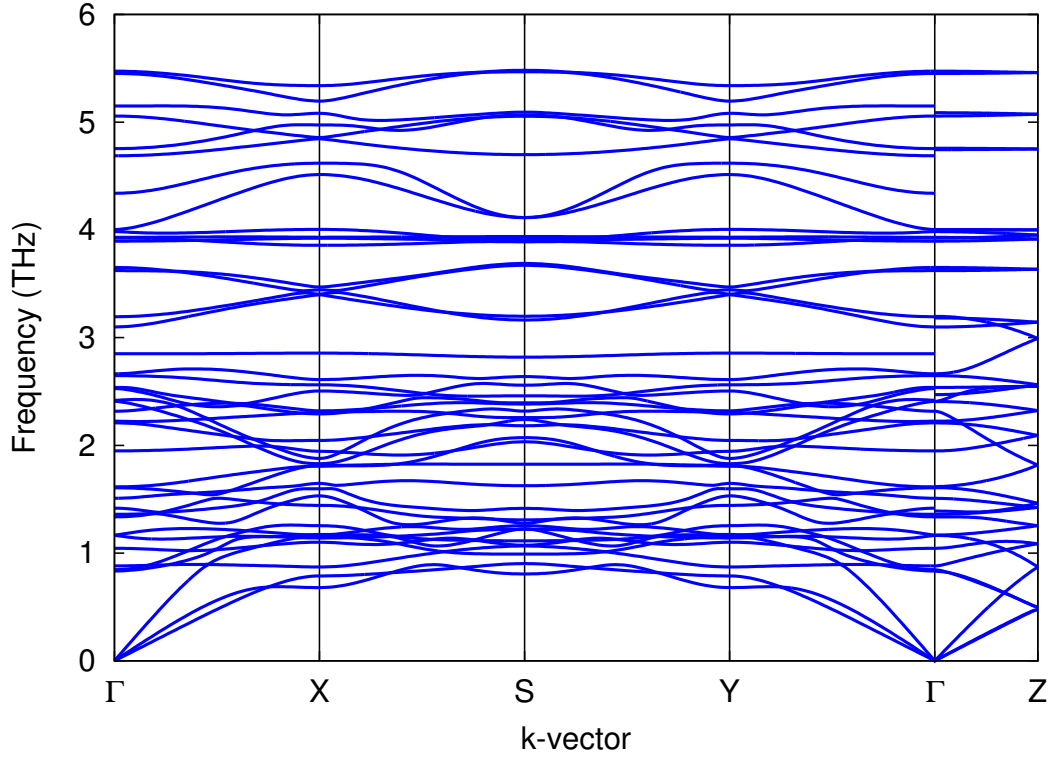


FIG. 2: Phonon dispersion relations of BaIn₂Te₄.

atoms, which is the heaviest atom in the BaIn₂Te₄ material, is only in the 0-3 THz region, and the contribution of indium atoms is mostly between the 1-2 THz and 4-6 THz frequency regions. Since the mass of In and Te atoms are very close to each other, we encounter strong degeneracy between two atoms. These degeneracies occur both in the high optical region (>3.8 THz) and in acoustic-low optical region (around 1 THz region).

The temperature dependence of lattice thermal conductivity calculated from Eqn. 4 is shown in Fig. 4 along x , y , and z directions. For all temperatures, the lattice thermal conductivity in the x -direction (where 1D-chains comprise) is found about 1.7 and 1.8 times larger compared to y - and z -directions, respectively. Fig. 4 also shows total thermal conductivity ($\kappa_{top} = \kappa_l + \kappa_e$) reported by Ishtiyak *et al.*[27]. As a result of that the electronic conductivity is negligibly low compared to the lattice thermal conductivity in many (undoped) semiconductor materials, we can directly compare the calculated κ_l values with the experimental result. As seen from the figure, calculated the average lattice thermal conductivity is very close to the experimental values.

To present our understanding of the mechanisms underlying the low thermal conductivity

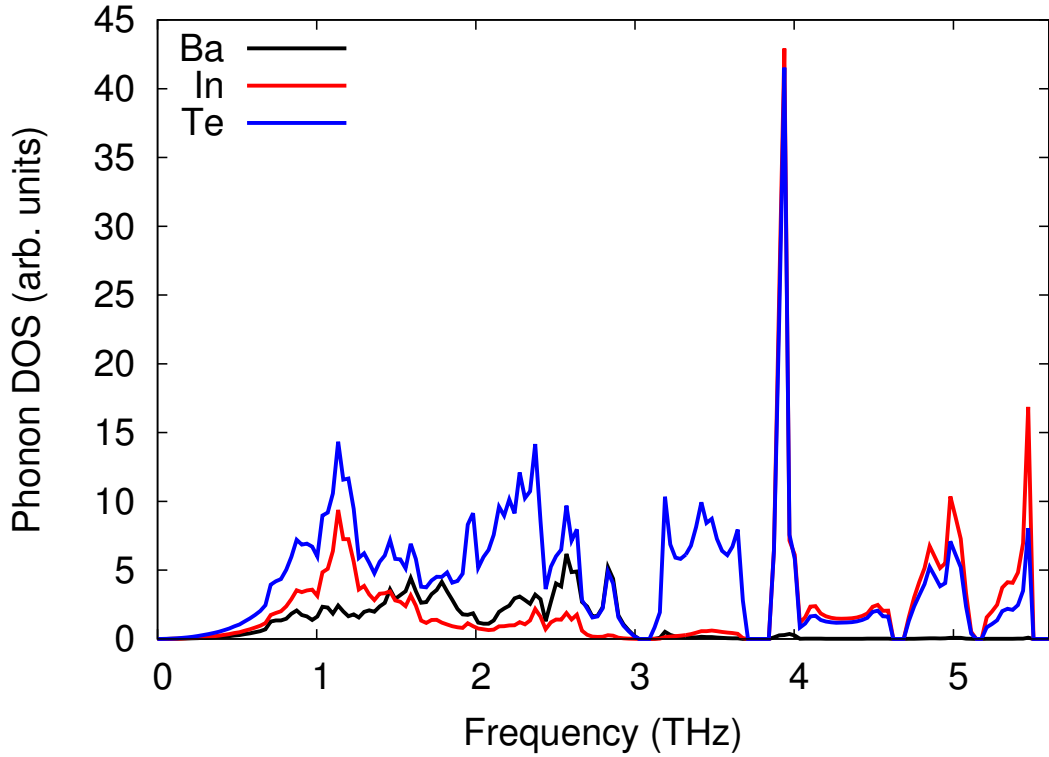


FIG. 3: Total and partial phonon density of states of BaIn_2Te_4 .

behavior of BaIn_2Te_4 , mode Grüneisen parameters, phonon group velocities, and anharmonic scattering rates are shown in Figs. 5a, b, and c, respectively. Anharmonicity of a periodic crystal can be partially characterized by the mode Grüneisen parameters. Indeed, a large Grüneisen parameter usually points out a strong anharmonicity. As seen in Fig. 5a, the predicted large negative Grüneisen parameters, up to value of -3, for some acoustic modes and low frequency (< 2 THz) optical modes are parallel with this statement and indicate a strong anharmonicity of phonons in BaIn_2Te_4 .

Fig. 5b shows the phonon group velocities of BaIn_2Te_4 as a function of frequency. In the acoustic region, values up to 3 km/s corresponds to LA modes only and group velocities of TA modes do not exceed 1.5 km/s. The low TA group velocities and hence sound velocities lead to soft elastic moduli (Supplemental Material Table S1[45]) and low bulk modulus (Table I). As a trend, optical modes are expected to have lower group velocities than acoustic modes and their effect on thermal conductivity involve much less contribution. The phonon group velocities of optical modes mostly do not exceed 1-1.2 km/s. But it was found that the group velocities of the highly dispersed optical modes around 3 THz and 4.5 THz region are

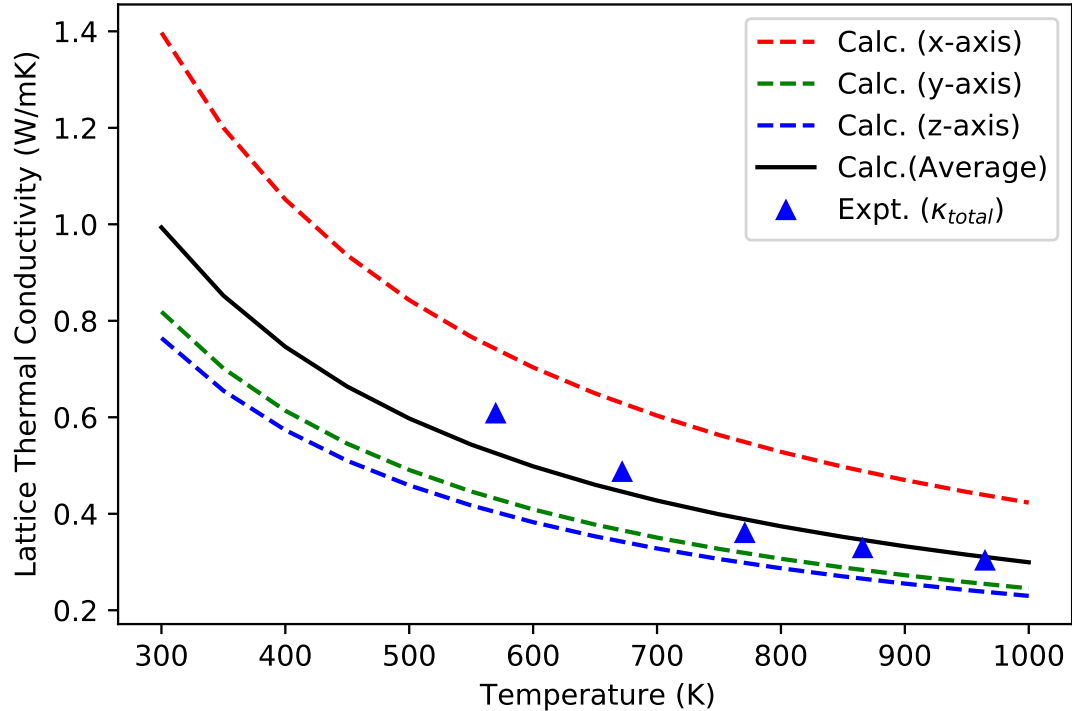


FIG. 4: Lattice thermal conductivity of BaIn_2Te_4 along x , y , and z directions together with the average value. The experimental measurement is taken from Ref.[27].

higher than the other optical modes. These high group velocities have small contribution to the lattice thermal conductivity, particularly in x direction (Fig. 6) as discussed below. The phonon group velocities of BaIn_2Te_4 material are found to be significantly lower than the group velocities of the thermoelectric PbTe material[51] which is well known for having low thermal conductivity. Thus, it is clear that low group velocities play a significant role for understanding the low lattice thermal conductivity of BaIn_2Te_4 material.

Another important factor affecting the lattice thermal conductivity is the anharmonic scattering rates and the calculated values at 300 K are shown in Fig. 5c as a function of frequency. Low anharmonic scattering rates reflect larger relaxation times and greatly increase the lattice thermal conductivity and as can be seen from the figure, the smallest values are in the 0-1 THz acoustic region. High-frequency optical phonons mostly exhibit large scattering rates compared to acoustic modes. Nevertheless, some scattering rate values in the optical region (particularly around 4 THz) are also quite low which cause a notable

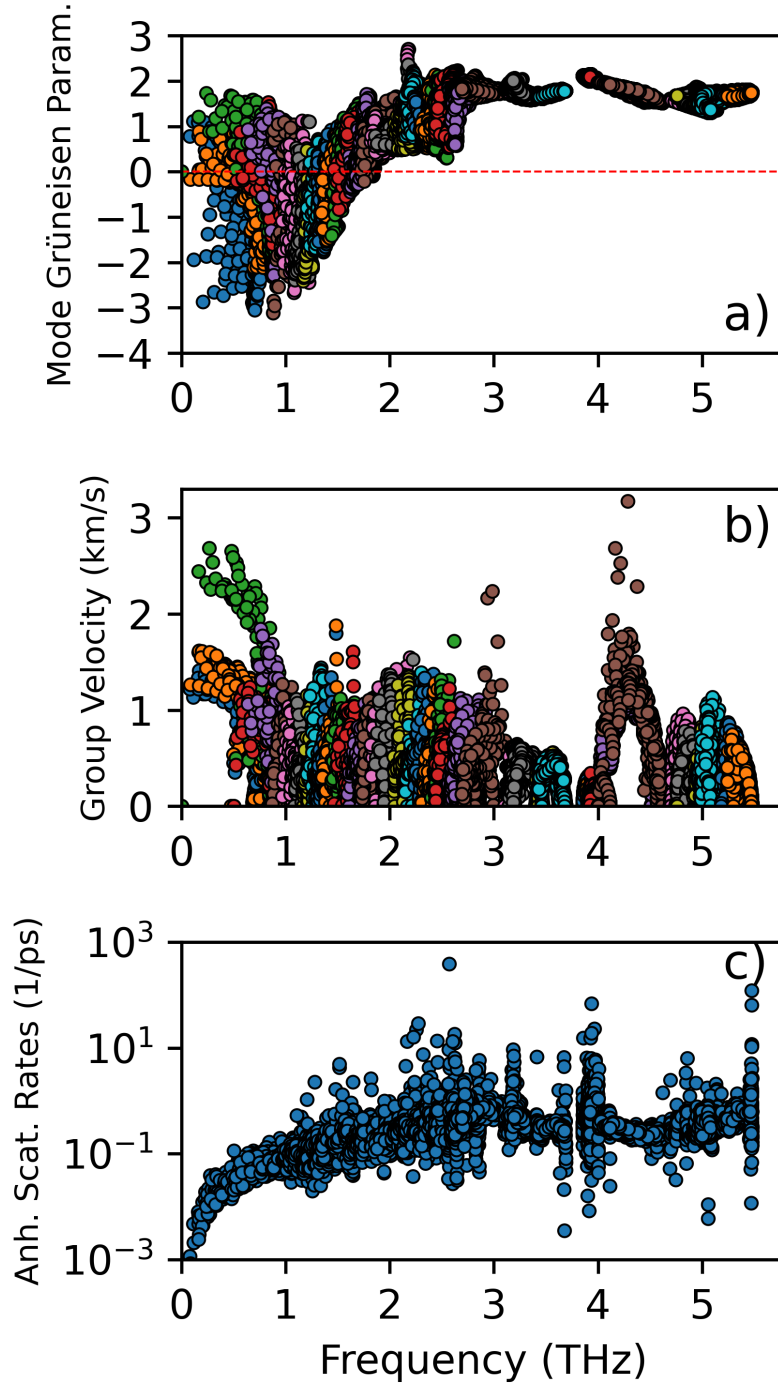


FIG. 5: The calculated (a) mode Grüneisen parameters, (b) phonon group velocities, and (c) anharmonic scattering rates of BaIn_2Te_4 .

increment in the lattice thermal conductivity.

The cumulative lattice thermal conductivity is another useful quantity which manifests

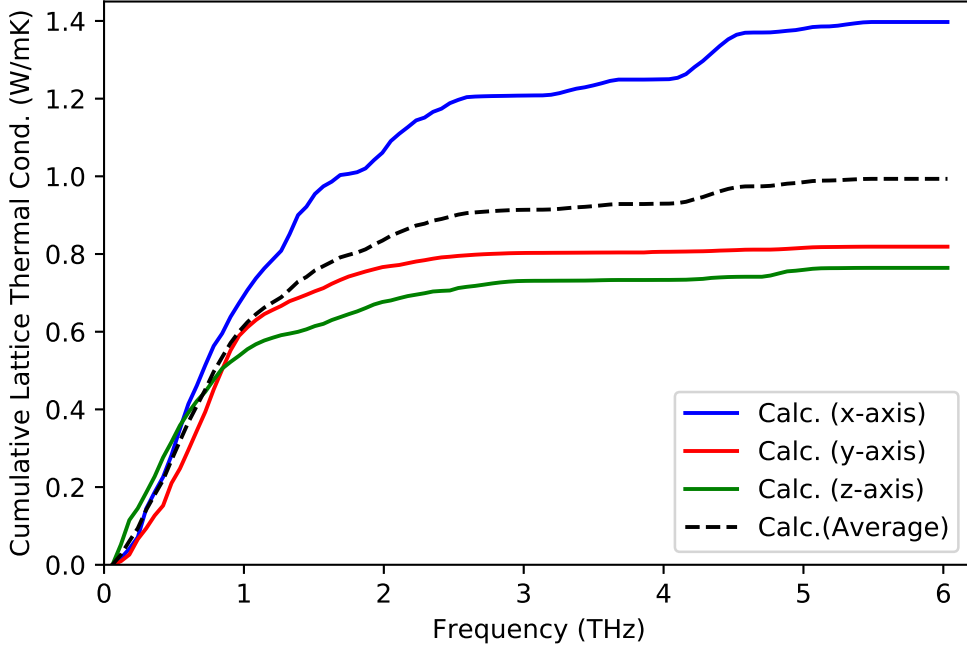


FIG. 6: The cumulative lattice thermal conductivity calculated at 300 K for BaIn_2Te_4 along x , y , and z directions together with the average value.

the contribution of phonons with different frequencies to the total thermal conductivity. Fig. 6 shows the cumulative lattice thermal conductivity as a function of the phonon frequency at room temperature (300 K). As can be seen from the figure, almost all of the contributions to the average lattice thermal conductivity come from the 0-2 THz frequency region, while the contribution from the 0-1 THz region is around 60%. The major contribution of the optical regions comes from the x -direction (the 1D-chain direction), while contributions in y - and z -directions are very small.

C. Electronic Properties

Using the GGA and GGA+SOC optimized structures, the electronic band structure of BaIn_2Te_4 in the frameworks of GGA-PBE and GGA-PBE-SOC were calculated along the high symmetry directions of the Brillouin zone of the orthorhombic lattice. In addition, the HSE06 hybrid functional correction was applied to correct the failure of GGA-PBE in determination of band-gap of semiconductor systems. The obtained results are displayed in

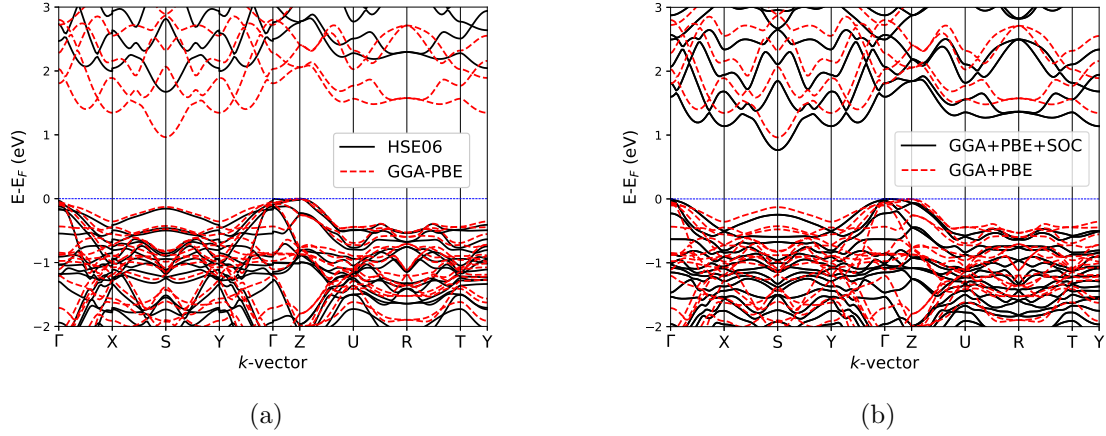


FIG. 7: Electronic band structure of BaIn_2Te_4 calculated with (a) HSE06 (full lines) and GGA-PBE (dashed lines) (b) GGA-PBE-SOC (full lines) and GGA-PBE (dashed lines).

The Fermi level is set to 0 eV.

Fig. 7. The valence band maximum is located at Z point and the conduction band minimum is located at S point, resulting an indirect band gap (S - Z) values of 0.963 and 1.670 eV for GGA-PBE and HSE06, respectively (Fig. 7a). For the GGA-PBE-SOC case, the valence band maximum is located at Γ point with a lower indirect band gap 0.76 eV (Fig. 7b). The direct bandgap at Γ high-symmetry point is predicted as about 1.85 eV for GGA-PBE and 2.5 eV for HSE06. The direct band gap of the GGA-PBE-SOC calculation is found to be 1.6 eV. To the best of our knowledge, the only experimental determination of the band gap is performed in the study of Ishiyak et. al.[27] for polycrystalline sample of BaIn_2Te_4 . In their optical absorption study at room temperature, they estimated the indirect and direct band gap values as 0.83 eV (or lower) and 1.36 eV, respectively. These values are quite small when compared to our calculations. They stated that the obtained values remained within the limits of the spectrophotometer they used. In fact, our calculations point out that the experimental limitations might have significant influence on reported values. Therefore, further complementary experimental electronic structure studies are required in this regard.

One important behavior of the band structure of BaIn_2Te_4 is having close valence extremum of Γ , Z and S points including two- or three-fold band degeneracy containing heavy bands. These are the indication of intrinsically large Seebeck coefficients which leads to the higher power factor of the material[52]. By considering that the bands of GGA-PBE and

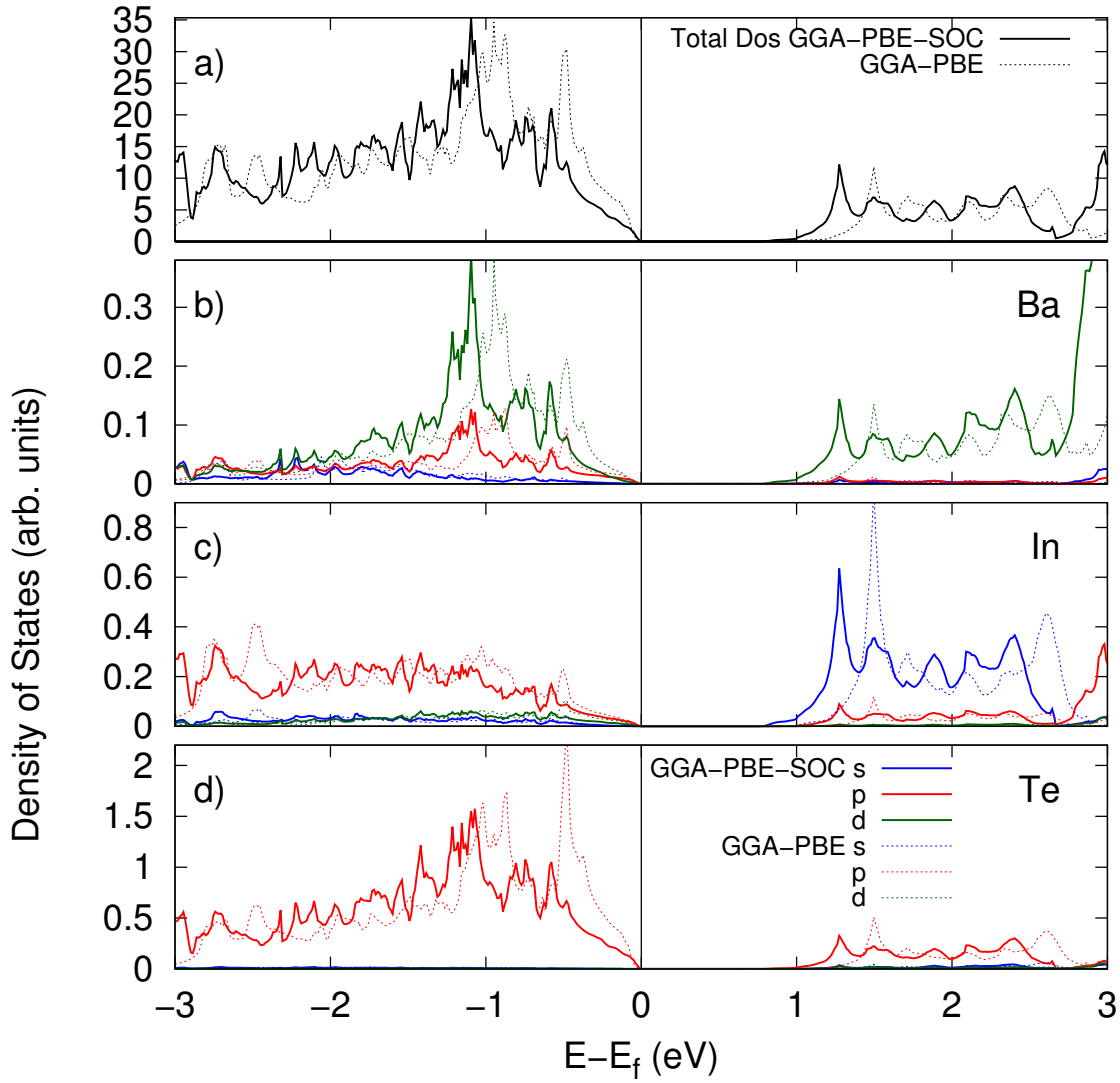


FIG. 8: Electronic density of states of BaIn_2Te_4 calculated with GGA-PBE-SOC (full lines) and GGA-PBE (dotted lines). (a) Total density of states and partial density of states of atoms (b) barium, (c) indium, and (d) tellurium. The Fermi level is set to 0 eV.

HSE06 do not change too much except the band gap, for the subsequent calculations, we have used the GGA-PBE and GGA-PBE-SOC methods and applied a scissor operator to the band gap in the sense of rigid band approximation. We set the band gap to the HSE06 value for electron transport calculations.

The calculated GGA-PBE and GGA-PBE-SOC partial and total density of states (DOS) of orthorhombic BaIn_2Te_4 are shown in Fig. 8. The valence band near Fermi level are formed

mainly by Te-5*p* orbitals together with minor contributions from Ba-4*d* and Ba-5*p* states and the conduction band is composed of the In-5*s* and Ba-4*d* orbitals. The In atoms only denote in conduction band and no obvious contribution to the valence states. It may be expected that the *p*-type doping and alloying on In sites would minimally affect the valance band structure and hence the mobility which are very important for thermoelectric performance. The large slope of the total DOS (Fig. 8a) in the valence band near Fermi level also suggests large Seebeck coefficients together with the possible use of the BaIn₂Te₄ material as a *p*-type thermoelectric material. As shown in figure, the GGA-PBE-SOC results meaningfully lower this slope compared to GGA-PBE which is an indication of that the spin-orbit interactions can not be neglected.

D. Thermoelectric Properties

Before starting to discuss the thermoelectric properties, it is convenient to investigate carrier scattering rates and mobility where the GGA-PBE-SOC results are given in Fig. 9 at 300 K with a 10^{19} cm⁻³ carrier concentration. The calculated scattering rates as a function of energy are shown in Fig. 9a and Fig. 9b for *p*-type (hole doping) and *n*-type (electron doping), respectively. It is clearly seen that polar-optical scattering rates have highest values followed by the impurity scattering. ADP scatterings have lowest values, particularly at energies through the band edges. Fig. 9c and Fig. 9d present the total and scattering type resolved mobilities with respect to temperature for *p*-type and *n*-type doping, respectively. We have found that the POP scattering is the dominant scattering for both doping types. This behavior have also been found in many well known thermoelectric materials PbTe[53], SnS[54], SnSe[55], and in many complex materials[32, 56–59]. Both total, POP, and ADP mobility decreases with increasing temperature and the IMP scattering is almost independent of temperature.

Fig. 10 presents the calculated Seebeck coefficients, electrical conductivity, and electronic thermal conductivity with respect to carrier concentration for both *p*-type and *n*-type doping. Both GGA-PBE and GGA-PBE-SOC calculations are presented for comparison. All results are given as the average of *x*, *y*, and *z* directions. The direction oriented results can be found in Fig. S1 of Supplemental Material[45]. For both types of doping, the Seebeck coefficients increase with temperature and decrease with carrier concentration as shown in Figs. 10a

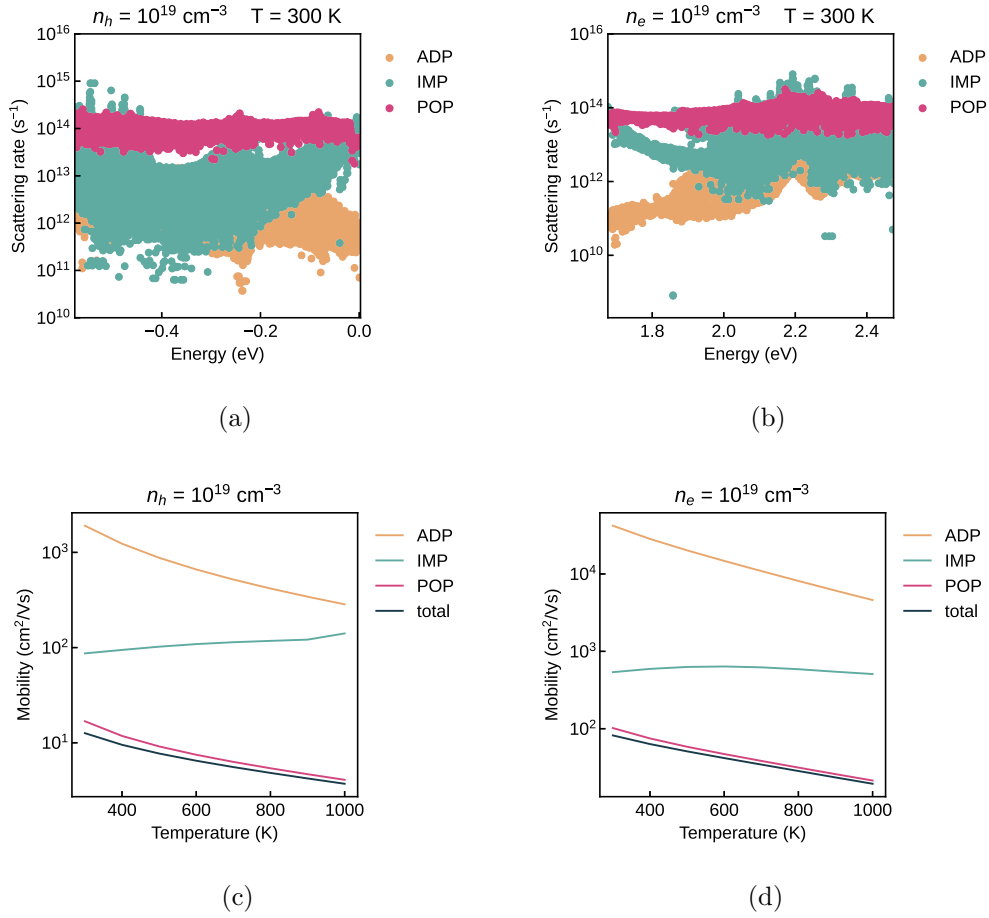


FIG. 9: The total and scattering mechanism resolved room temperature electronic scattering rates for (a) hole doping and for (b) electron doping calculated with GGA-PBE-SOC. The total and scattering mechanism resolved mobility as a function of temperature for (c) hole doping and for (d) electron doping. All the results are given at 10^{19} cm^{-3} carrier concentration.

and 10d. The *p*-type Seebeck coefficient is more than 1.5 times larger compared the *n*-type system considering the same carrier concentration. Spin-orbit interactions is found to be lower *p*-type Seebeck coefficients about 10% in average while *n*-type Seebeck coefficients are not effected. Since the electrical conductivity (σ) is given as $\sigma = ne\mu$, where n is the carrier concentration, e is the unit charge, and μ is the mobility, we find that electrical conductivity increases with increasing carrier concentration for both types of doping (Figs. 10b and 10e). Electrical conductivity decreases with temperature due to the strengthening of scattering mechanisms at high temperatures. The *n*-type electric conductivity is found to be several

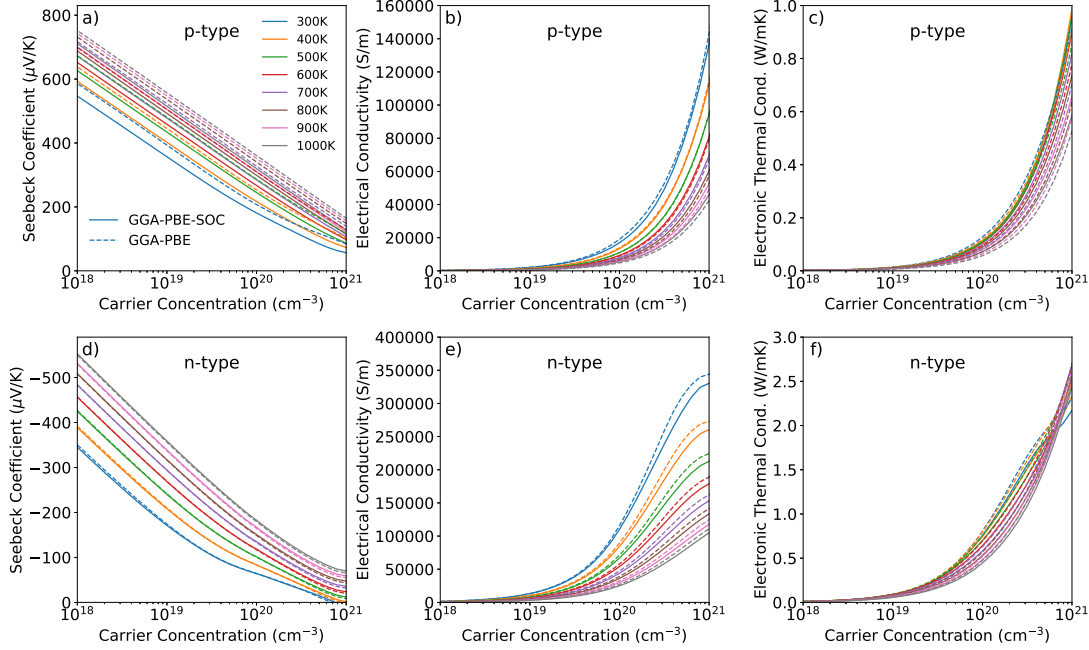


FIG. 10: Electronic transport properties of BaIn_2Te_4 calculated with GGA-PBE-SOC (full lines) and GGA-PBE (dashed lines) as a function of carrier concentration with temperatures in the range of 300-1000 K. (a) Seebeck coefficient, (b) electrical conductivity, (c) electronic thermal conductivity for p -type system and (d) Seebeck coefficient, (e) electrical conductivity, (f) electronic thermal conductivity for n -type system.

times larger than those of p -type doping. As an example, at 300 K and 10^{20} cm^{-3} carrier concentration, the electrical conductivity of n -type doping is about six times larger than the p -type system. Inclusion of spin-orbit interactions cause a slight decrease in the n -type electrical conductivity.

We see from Figs. 10c and 10f that the electronic thermal conductivity (κ_e) is slightly effected inclusion of SOC. κ_e increases with increasing carrier concentration and can reach to 0.5-0.9 (2.3-2.7) W/mK values for p -type (n -type) systems at 10^{21} cm^{-3} carrier concentrations in a 300-1000 K range. Due to the increasing scattering processes at high temperatures, electronic thermal conductivity decreases with increasing temperature. But at higher concentrations, the p -type κ_e is at the order of lattice thermal conductivity and the n -type κ_e largely exceeds lattice thermal conductivity. This behavior is unfavorable for a high ZT especially for the n -type system.

The power factor ($PF=S^2\sigma$) as a function of carrier concentration given with various temperatures helps us to investigate the optimal doping for a good thermoelectric behavior in the framework of the electronic transport. We present the direction averaged results in Figs. 11a and 11c for p -type and n -type dopings, respectively. The direction oriented results can be found in Figs. S2a and S2c of the Supplemental Material[45]. The opposite behavior of Seebeck coefficients and electrical conductivity with respect to carrier concentration leads the higher PF values at moderate concentrations. The highest PF is found at carrier concentrations close to 10^{21} cm^{-3} for p -type doping and 10^{20} cm^{-3} for n -type doping. The reduction of p -type Seebeck coefficients on SOC calculations largely reduce the p -type power factors. The decrement of PF caused by SOC is quite small in the n -type system as the reduction in electrical conductivity is small. As considering SOC results, despite the lower electrical conductivity of p -type doping, owing to its higher Seebeck coefficient, PF of p -type system is found on a small scale higher compared to n -type system. For the n -type system, increment of the highest PF value with increasing temperature is found to be shorten. Moreover, for p -type system, the highest PF value increases from temperatures 300 K to 600 K and then starts to decrease due to the decrement of electrical conductivity together with the similar values of high temperature Seebeck coefficients. For the temperatures between 300 K and 1000 K, the PF values are obtained in the range of 0.6-0.9 mW/mK^2 for p -type and 0.4-0.8 mW/mK^2 for n -type doping. We can conclude that our p -type PF highest values are moderate compared to well known thermoelectric p -doped telluride $\text{Sn}_{1-x}\text{Mn}_x\text{Te}$ [60] with highest PF values obtained around 2 mW/mK^2 .

After a detailed investigation of the thermoelectric transport properties, combined with the calculated lattice thermal conductivity, we predicted the average ZT of BaIn_2Te_4 with respect to carrier concentration and temperatures in a range 300-1000 K. The results calculated with GGA-PBE and GGA-PBE-SOC are given in Figs. 11b and 11d for p -type and n -type dopings, respectively. The direction oriented results can also be found in Figs. S2b and S2d of the Supplemental Material[45]. Due to the increasing behavior of electronic thermal conductivity with respect to carrier concentration, the highest predicted ZT values are obtained at somewhat lower concentrations compared to highest PFs. The spin-orbit interactions strongly effect the p -type ZT values. In the framework of SOC included calculations, the highest predicted ZT is calculated to be around 2×10^{20} cm^{-3} for p -type and around 3.2×10^{19} cm^{-3} for n -type systems. In the p -type system, the maximum ZT

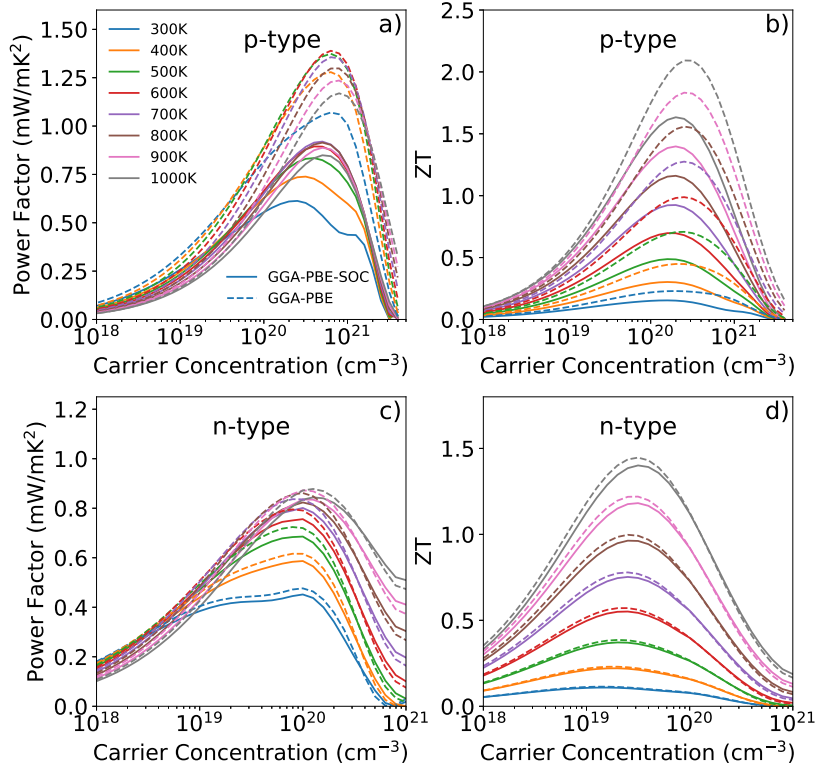


FIG. 11: Power factor and ZT of BaIn_2Te_4 calculated with GGA-PBE-SOC (full lines) and GGA-PBE (dashed lines) as a function of carrier concentration with temperatures in the range of 300-1000 K. (a) Power factor and (b) ZT of p -type system, and (c) power factor and (d) ZT of n -type system.

exceeds unity after 700 K and reaches to 1.63 value at 1000 K. In the case of n -type doping, maximum ZT exceeds unity after 800 K and reaches to 1.40 value at 1000 K. Our p -type predicted ZT value at 900 K is 1.4 and this value is larger than the experimentally obtained 1.3 value for p -doped $\text{Sn}_{1-x}\text{Mn}_x\text{Te}$ [60] at the same temperature. Together with the moderate PF values of BaIn_2Te_4 , the predicted high ZT values are achieved because of its low lattice thermal conductivity. By considering the anisotropic behavior of the electronic transport properties (Supplemental Material Fig. S1[45]) together with the anisotropy of lattice thermal conductivity (Fig. 4), we also predicted higher ZT values along y -direction with 1.76 for p -type and along z -direction 1.76 for n -type systems at 1000 K (Supplemental Material Fig. S2[45]).

IV. CONCLUSION

The average lattice thermal conductivity values calculated based on the first principles solution of the linearized phonon Boltzmann transport equation for different temperatures are in very good agreement with the experimentally measured ones. The detailed investigations show that (i) high-negative mode Grüneisen parameters, (ii) extremely low phonon group velocities of particularly acoustic modes, and (iii) high phonon scattering rates at low-frequency regions due to the hybridization of low optical modes with LA modes can be considered as the main sources of the predicted low lattice thermal conductivity. Apart from that, we determined the semi-one dimensional chain structure within the crystal has a notable influence on lattice thermal transport and results in highly anisotropic transport properties: the lattice thermal conductivity in the x -direction was found to be approximately 1.7 (1.8) times larger than in the y (z) directions.

The calculated band gap values with both regular and semi-corrected functional highly conflict with the available measurements and these results clearly point out further experimental research in that sense. Seebeck coefficients of p -type doped BaIn_2Te_4 material exhibit much larger values than the n -type material at the same concentration while the electrical conductivity value of n -type material is found much larger than the p -type system. We also report that the spin-orbit coupling effects can not be ignored for the thermoelectric properties, especially for the p -type system.

More importantly, along with the analysis of the thermoelectric properties, we predict that the orthorhombic BaIn_2Te_4 exhibit high ZT values desired for technological applications and this material can be considered a superior thermoelectric material with both p -type and n -type doping. Note that, the highest ZT values are predicted along the off-chain y -direction for p -type doping and z -direction for n -type doping. This material can be further investigated via Spark Plasma Sintering fabrication and Chemical Doping to completely figure out its thermoelectric potential of it.

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